

The two formulae implemented for the red and blue curves of figure 8 of the note (up to an irrelevant overall normalization factor K that is the same for both) are

$$\frac{dN^{GLV}}{dx_+}(x_+) = K \frac{1}{x_+} \int_0^{\sqrt{3\mu E}} q dq \frac{1}{(4x_+ E \hbar c/L)^2 + q^4} \int_0^{2x_+(1-x_+)E} k dk \frac{k^2 - q^2 + \mu^2}{[(k-q)^2 + \mu^2]^{3/2} [(k+q)^2 + \mu^2]^{3/2}}; \quad (1)$$

$$\frac{dN^{ASW}}{dx_E}(x_E) = K \frac{1}{x_E} \int_0^{\sqrt{3\mu E}} q dq \frac{1}{(4x_E E \hbar c/L)^2 + q^4} \int_0^{x_E E} k dk \frac{k^2 - q^2 + \mu^2}{[(k-q)^2 + \mu^2]^{3/2} [(k+q)^2 + \mu^2]^{3/2}}. \quad (2)$$

First note that the two equations are identical in form. Also, in the eikonal limit $k_\perp \ll xE \Rightarrow x_+ \approx x_E$ and the integrands are identical; it is only in the k cutoff, where $k_\perp = xE$, that there is a difference in the formulae.

If I alter Eq. (1) such that the upper bound of the k integration does not include the $1 - x_+$ piece (specifically

$$\frac{dN^{GLV}}{dx_+}(x_+) = K \frac{1}{x_+} \int_0^{\sqrt{3\mu E}} q dq \frac{1}{(4x_+ E \hbar c/L)^2 + q^4} \int_0^{x_+ E} k dk \frac{k^2 - q^2 + \mu^2}{[(k-q)^2 + \mu^2]^{3/2} [(k+q)^2 + \mu^2]^{3/2}} \quad (3)$$

) and then plot this and Eq. (2) on the same graph, I get Fig. 1.

One can exploit the chain rule and the known inverses $x_+(x_E)$ and $x_E(x_+)$ to plot the two implementations on the same footing. Specifically

$$\frac{dN^{GLV}}{dx_E}(x_E) = \frac{dx_+}{dx_E} \frac{dN^{GLV}}{dx_+}(x_+(x_E)) \quad (4)$$

$$\frac{dN^{ASW}}{dx_+}(x_+) = \frac{dx_E}{dx_+} \frac{dN^{ASW}}{dx_E}(x_E(x_+)). \quad (5)$$

Fig. 2 shows $dN^{GLV}/dx_E(x_E)$ and $dN^{ASW}/dx_E(x_E)$. $dN^{GLV}/dx_+(x_+)$ and $dN^{ASW}/dx_+(x_+)$ are shown in Fig. 3. Note that for the previous two equations, the upper bound of the k integration is changed to reflect the new coordinates: for Eq. (4) the upper bound is $x_E E$; for Eq. (5), $2x_+ E$.

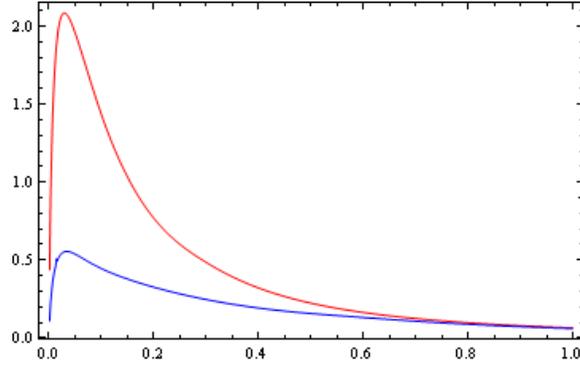


Figure 1: Eq. (3) in red and Eq. (2) in blue. Note that the “ x ” axis is not well defined; these are plots of $dN^{GLV}/dx_+(x_+)$ and $dN^{ASW}/dx_E(x_E)$ on the same graph. Other than the tail of the red curve (where $1 - x_+$ effects kick in) and an overall normalization factor, this is the same as Fig. 8 from the Cole Horowitz note.

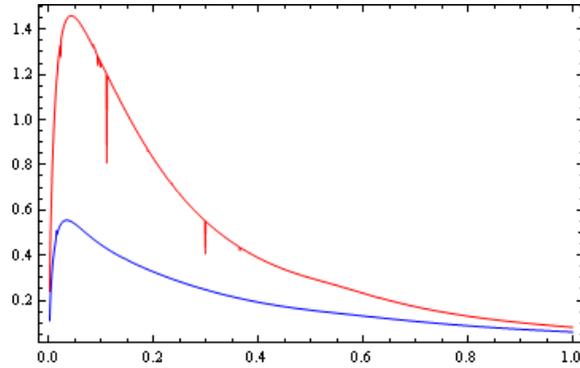


Figure 2: Plot of $dN^{GLV}/dx_E(x_E)$, Eq. (4), in red and $dN^{ASW}/dx_E(x_E)$, Eq. (2), in blue.

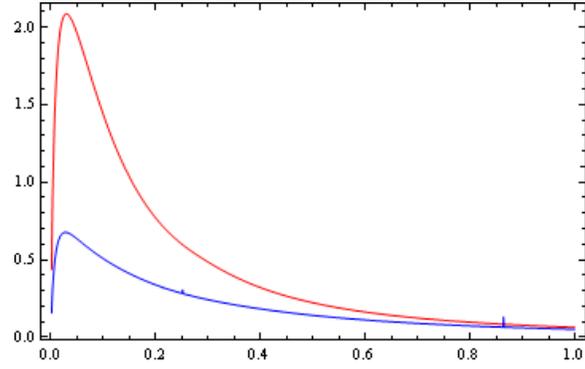


Figure 3: Plot of $dN^{GLV}/dx_+(x_+)$, Eq. (3), in red and $dN^{ASW}/dx_+(x_+)$, Eq. (5), in blue.