

“Development of a Spin-Light” Polarimeter for the EIC

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The Collaboration

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University of Virginia, Charlottesville, VA

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Argonne National Lab, Argonne, IL

David Gaskell (co-PI)

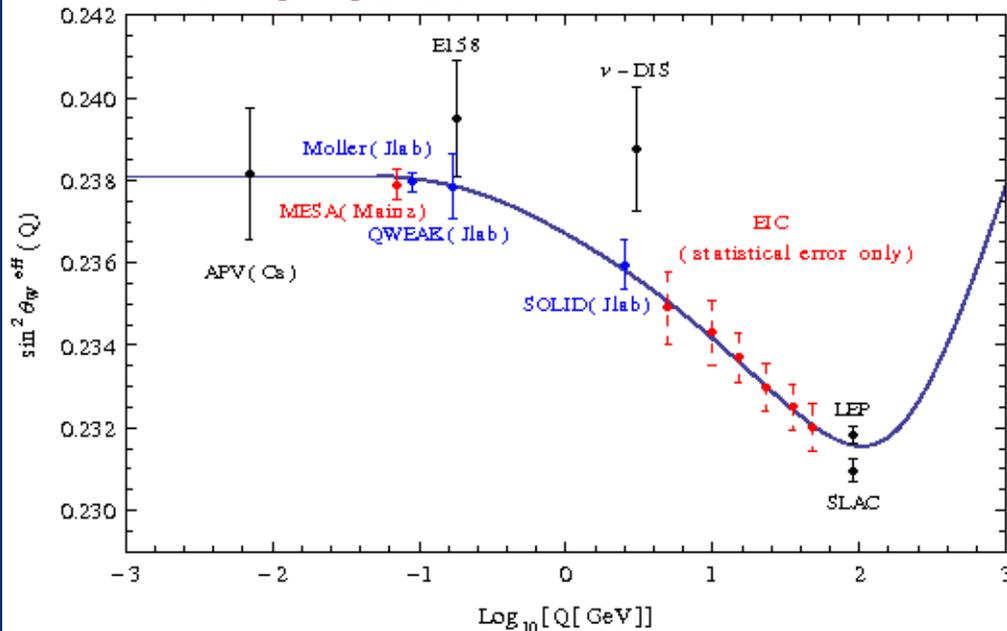
Thomas Jefferson National Accelerator Facility, Newport News, VA

The collaboration has extensive polarimetry and detector development experience at DESY, JLab, Mainz, and RHIC.

- **Introduction**
- **Synchrotron Radiation**
 - Classical & Quantum description
- **“Spin-Light”**
- **Conceptual Design of a “Spin-Light” polarimeter**
- **Detector and Prototype Development**
- **Summary**

The high energy and high luminosity polarized electrons, protons and ions at the EIC promises:

- a precise 3-D mapping of the proton's internal structure
- fundamental tests of QCD (such as Bjorken sum rule)
- tests of the SM at the quantum loop level that probe “new physics”



This entire program at the EIC requires precision electron polarimetry.

We propose to develop a novel continuous non-invasive polarimeter based on the spin dependence of synchrotron radiation (SR)

Projected uncertainties of future EIC measurements of $\sin^2 \theta_W$.

Synchrotron Radiation- “Electronic Light” 5

After its discovery, the angular and spectral distribution were worked out in classical E&M

Total Rate
$$P = \frac{dU}{dt} = \frac{2}{3} \frac{e^2 \gamma^4 c}{R^2}$$

$\gamma = \frac{E}{m_0 c^2}$: Lorentz boost

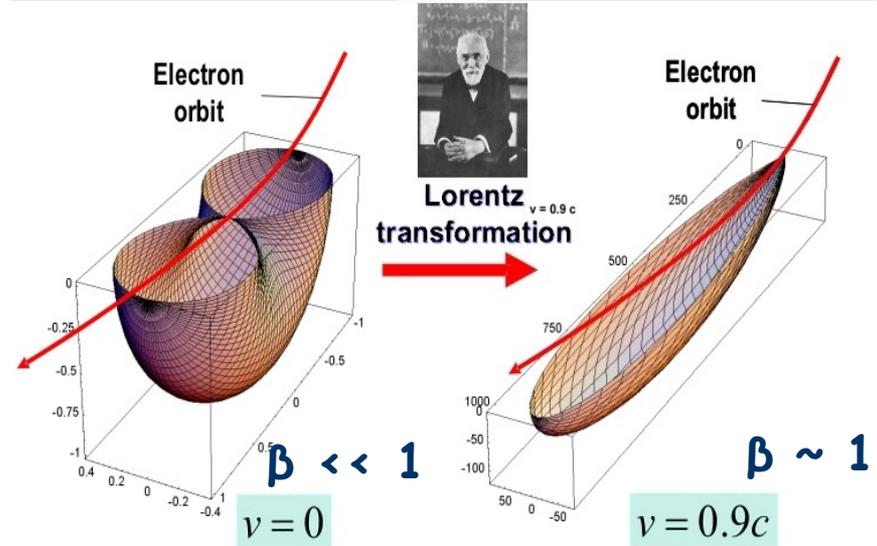
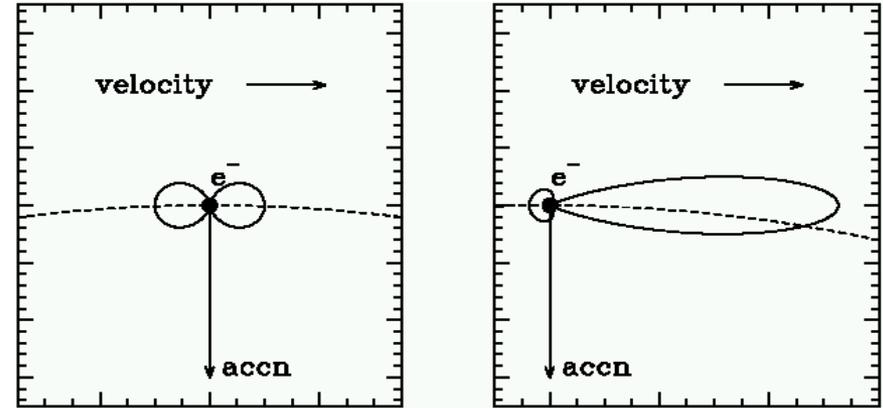
$$\frac{dU}{dt d\Omega} = \frac{e^2 \gamma^4 c}{4 \pi R^2} \frac{(1 - \beta \cos \theta)^2 - (1 - \beta^2) \sin^2 \theta \cos^2 \phi}{(1 - \beta \cos \theta)^5}$$

Angular distribution

For $\gamma \gg 1$ $\theta \sim 1/\gamma$

SR emitted in a very small cone

For $E_e = 11 \text{ GeV}$,
vert. size = $90 \mu\text{rad}$
i.e. 10m from the source $\sim 1 \text{ mm}$ height.



Synchrotron Radiation- "Electronic Light" ⁶

Quantum Corrections

Exact QED calculations by A.A. Sokolov and I. M. Ternov (1960s)

Classical theory (continuous SR spectrum) valid for

$$E \ll E_{\text{crit}} \sim 10^6 \text{ GeV} \quad \text{and} \quad B \ll B_{\text{crit}} \sim 4 \times 10^9 \text{ T}$$

E_{crit} : single SR photon carries away all of the electron's energy

Synchrotron Radiation- "Electronic Light" 7

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But even at lower energies

QED corrections \rightarrow spin dependence of the radiated power

$$P = P^{\text{clas}} \frac{9\sqrt{3}}{16\pi} \sum_{s'} \int \frac{y dy}{(1+\xi y)^4} I_{ss'}^2 F(y); \quad y = \frac{\omega}{\omega_c}; \quad \xi = \frac{3}{2} \frac{B}{B_{\text{crit}}} \gamma; \quad \begin{array}{l} s = \text{radial quantum \#} \\ I = \text{Laguerre func.} \\ \xi = \text{norm. B field strength} \end{array}$$

For $\xi \ll 1$ and electron spin $j, j' = \pm 1$

$$P = P^{\text{clas}} \left[\left(1 - \frac{55\sqrt{3}}{24} \xi + \frac{64}{3} \xi^2\right) - \left(\frac{1+jj'}{2}\right) \left(j\xi + \frac{5}{9} \xi^2 + \frac{245\sqrt{3}}{48} j\xi^2\right) + \left(\frac{1-jj'}{2}\right) \left(\frac{4}{3} \xi^2 + \frac{315\sqrt{3}}{432} j\xi^2\right) + \dots \right]$$

Synchrotron Radiation- "Electronic Light" 8

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spin dependent term

spin-flip dependent term

The Spin Dependence

To the first order in ξ the difference in SR intensity between polarized and unpolarized electrons is $\delta = \xi j \sim 10^{-4}$ for 100 μA , 5.0 GeV electrons

Verified experimentally at the VEPP-4 storage ring in Novosibirsk
Belomesthnykh et al., NIM 227, 173 (1984)

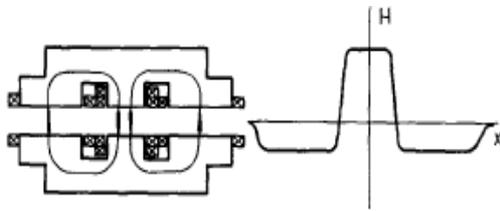


Fig. 1. The field vs the current in the 'snake'. A schematic of the 'snake' and the field distribution along its axis are shown below.

3 pole magnetic snake/wiggler

An RF field used to depolarize the electrons

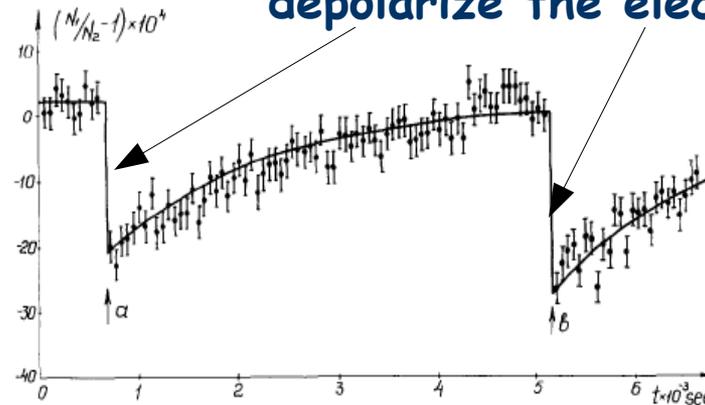


Fig. 12. The measurement results of the SR-intensity as a function of the degree of polarization of the beam. The field in the 'snake' coincides, in direction, with the storage ring guiding field. At points a and b one of the bunches (N_1), was quickly depolarized. The measurement time at a point is 60 s. The bunch polarization time is $\tau_p = 1740 \pm 20$ s ($\xi = 0.726$).

The spin-flip term contributes only as $\sim \xi^2$

This is responsible for the transverse self polarization of electron beams in storage rings: called the Sokolov-Ternov effect

Used to produce polarized electrons at various accelerator such as DESY

Longitudinal “Spin Light”

For longitudinally polarized electrons

Power from n_e electrons (ignoring spin flip and all terms $O(\xi^2)$)

$$P_y(\text{long}) = \frac{9 n_e c e^2}{16 \pi^3 R^2} \gamma^5 \int_0^\infty \frac{y^2 dy}{(1 + \xi y)^4} \oint d\Omega (1 + \alpha^2)^2 \left[K_{2/3}^2(z) + \frac{\alpha^2}{1 + \alpha^2} K_{1/3}^2(z) + j \xi y \frac{\alpha}{\sqrt{1 + \alpha^2}} K_{1/3}(z) K_{2/3}(z) \right]$$

R = bending radius, $y = \frac{\omega}{\omega_c}$; $\xi = \frac{3}{2} \frac{B}{B_{crit}} \gamma$; $\alpha = \gamma \psi$; $z = \frac{\omega}{2 \omega_c} (1 + \alpha^2)^{3/2}$; $K_{1/3}, K_{2/3}$ modified Bessel function

↑
vertical angle

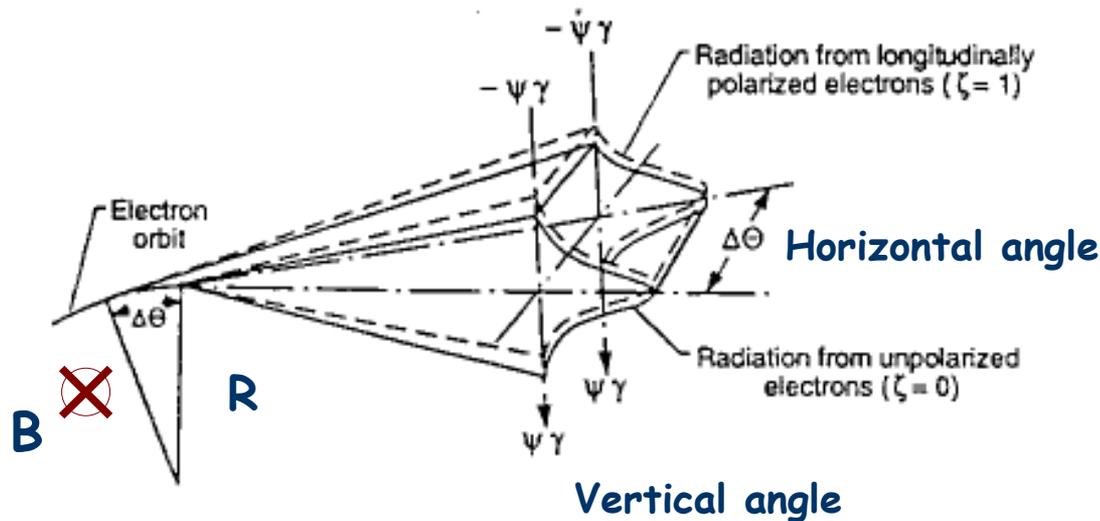


Figure 1: Geometrical definitions.

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↑
vertical angle

An odd function of the vertical angle

Integrated over all vertical angles the total SR power is spin **independent**

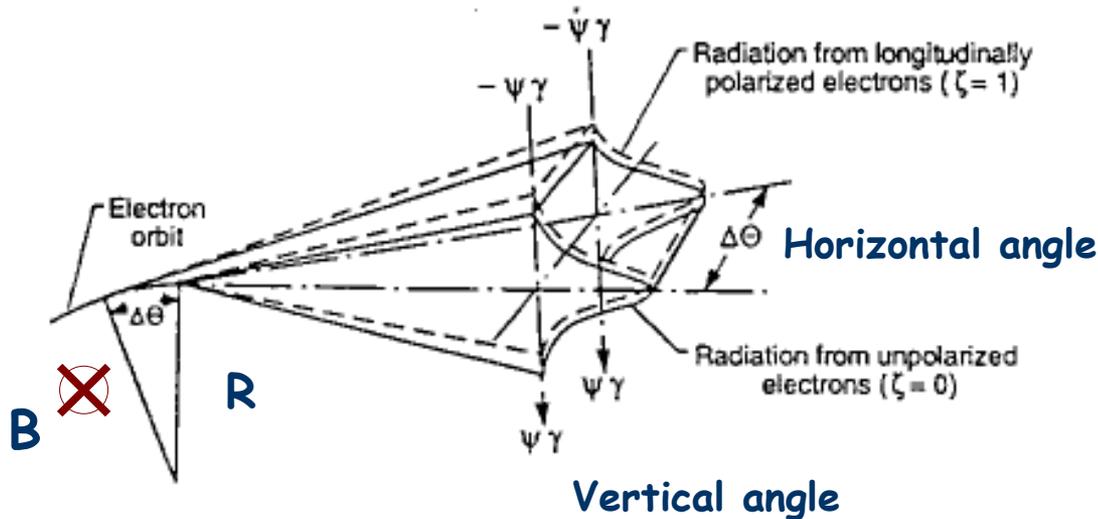
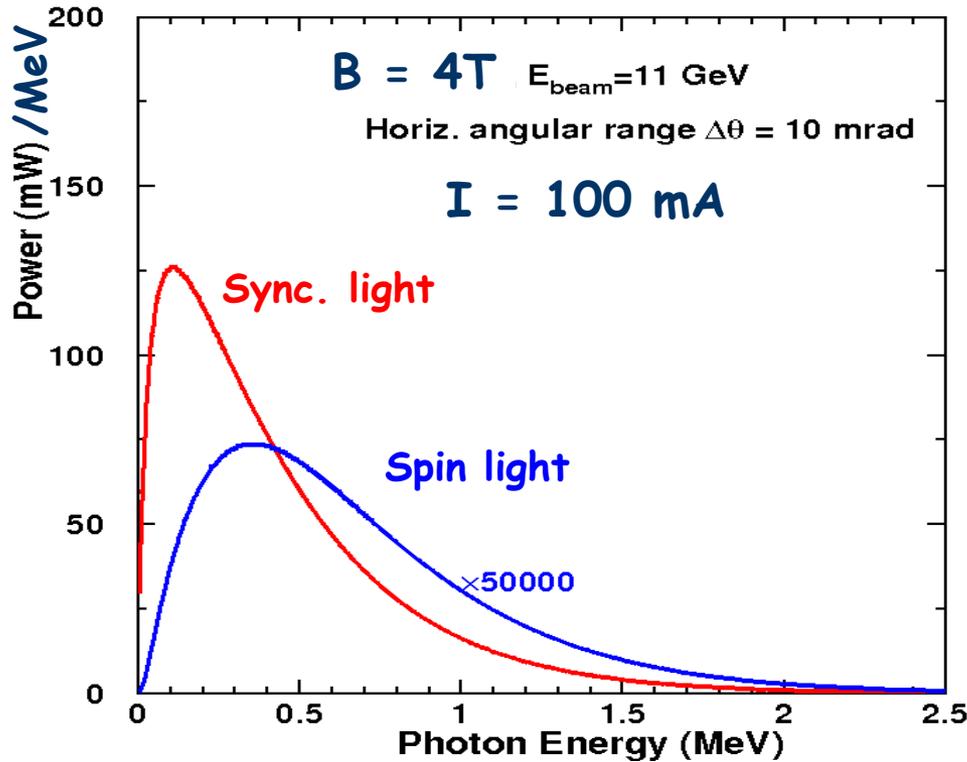


Figure 1: Geometrical definitions.

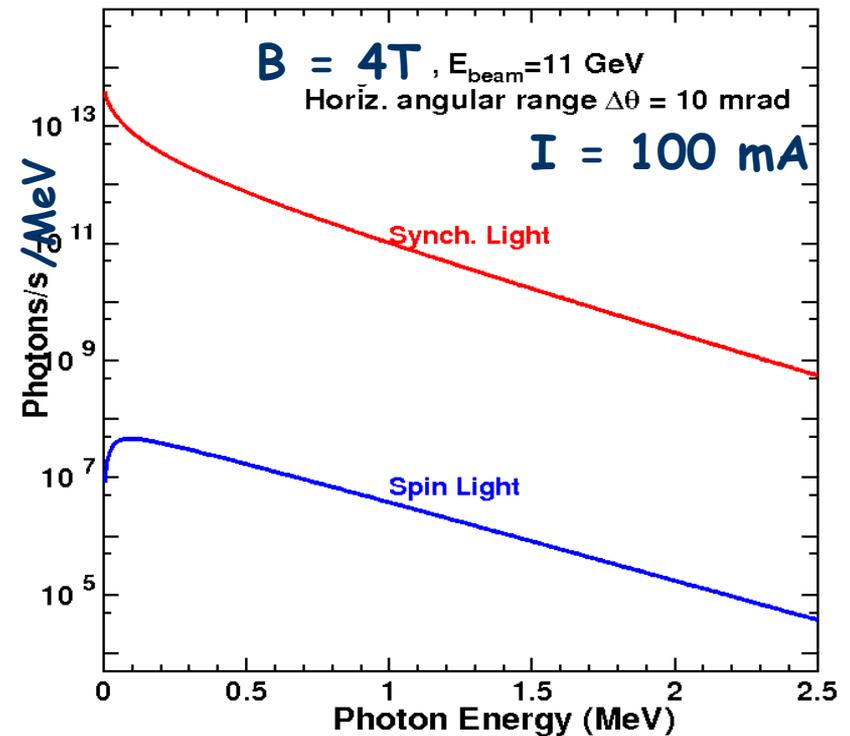
of photons radiated above and below the orbital plane are not equal

"Spin Light" - Some Characteristics



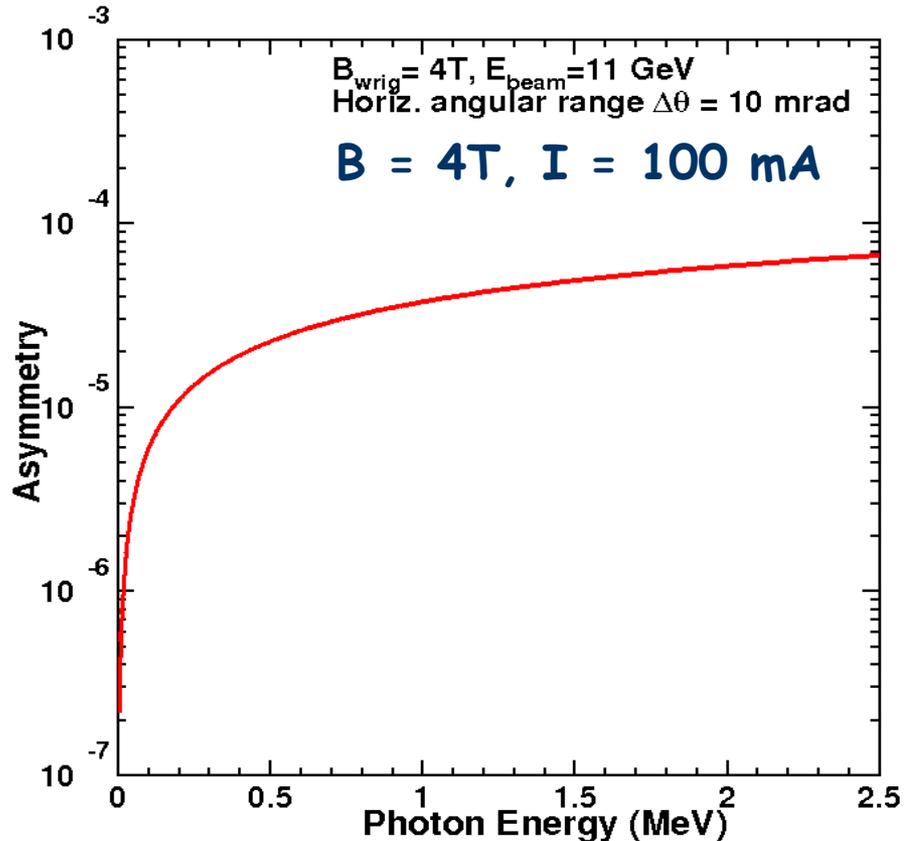
Radiated power peak at different frequencies for Sync vs Spin light

Number of photons/s
 $\sim 10^5$ different



“Spin Light” - Some Characteristics 13

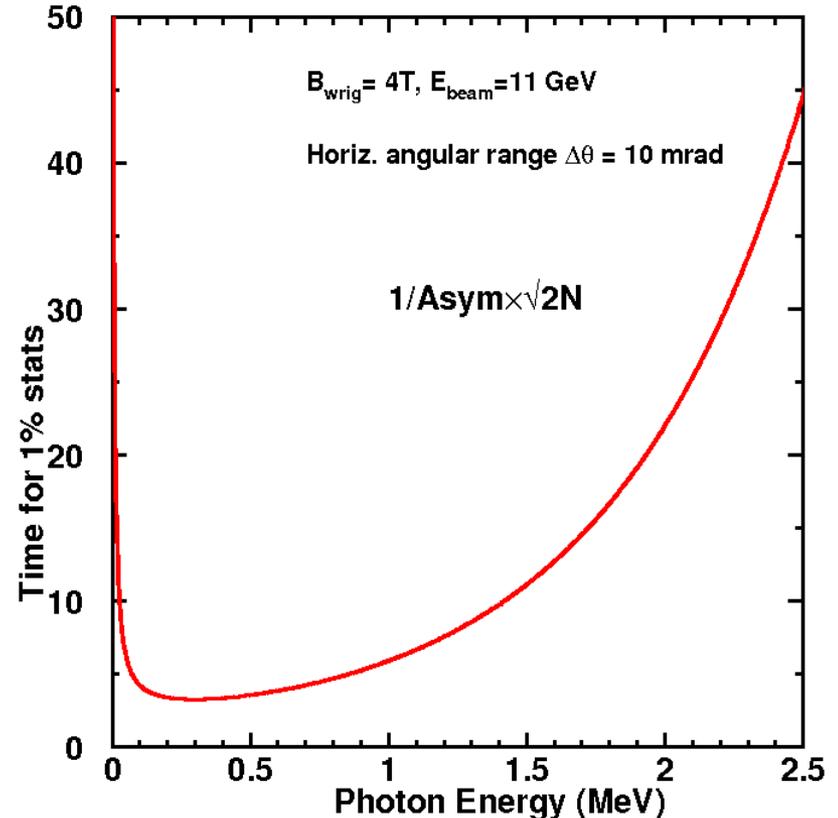
Asymmetry of number of photons
above and below the orbital plane



small asymmetry

But high rates imply
1% statistics in $\sim 10\text{ sec}$
Assuming Ion chambers efficiency $\sim 10\%$

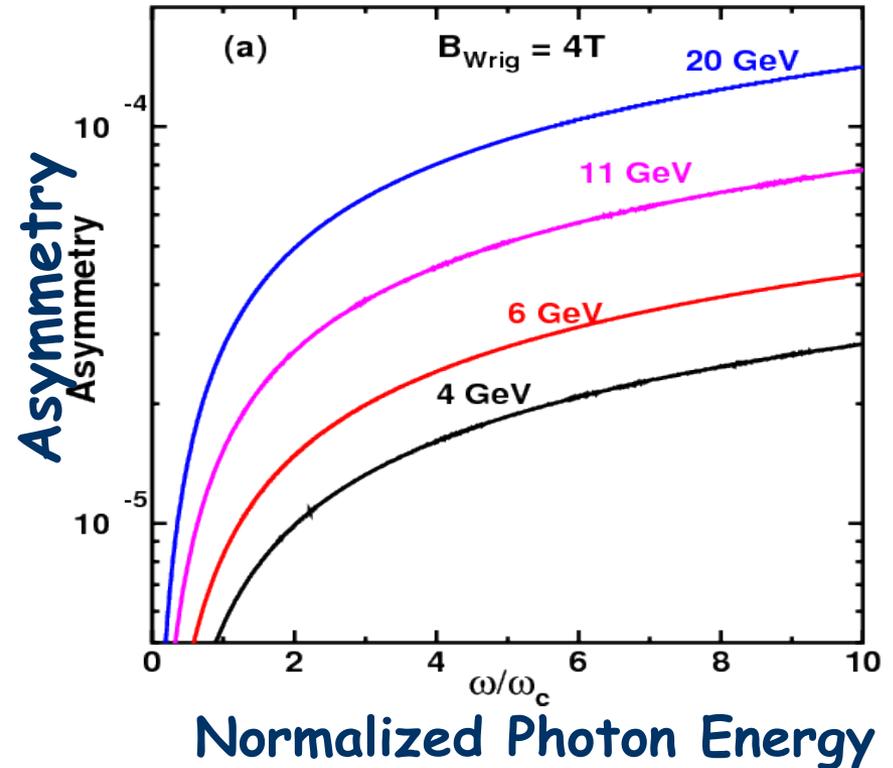
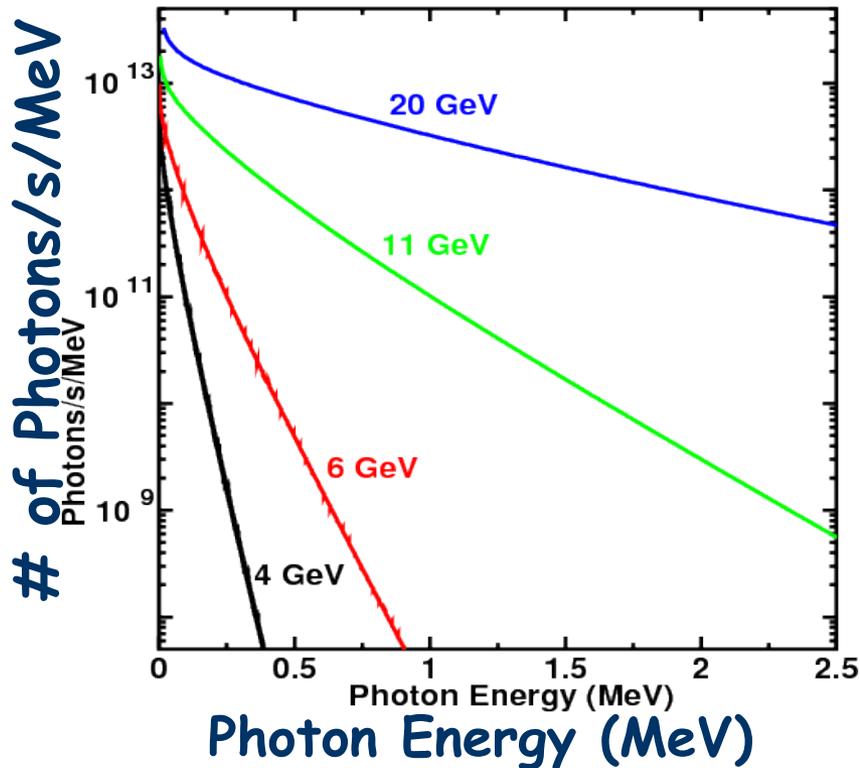
eat
eat



“Spin Light” - Energy Dependence

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At fixed $B = 4\text{T}$, $I = 100\text{ mA}$ and $\Delta\theta = 10\text{ mrad}$



of photons increases sharply with energy
but asymmetry increases slowly

Conceptual Design

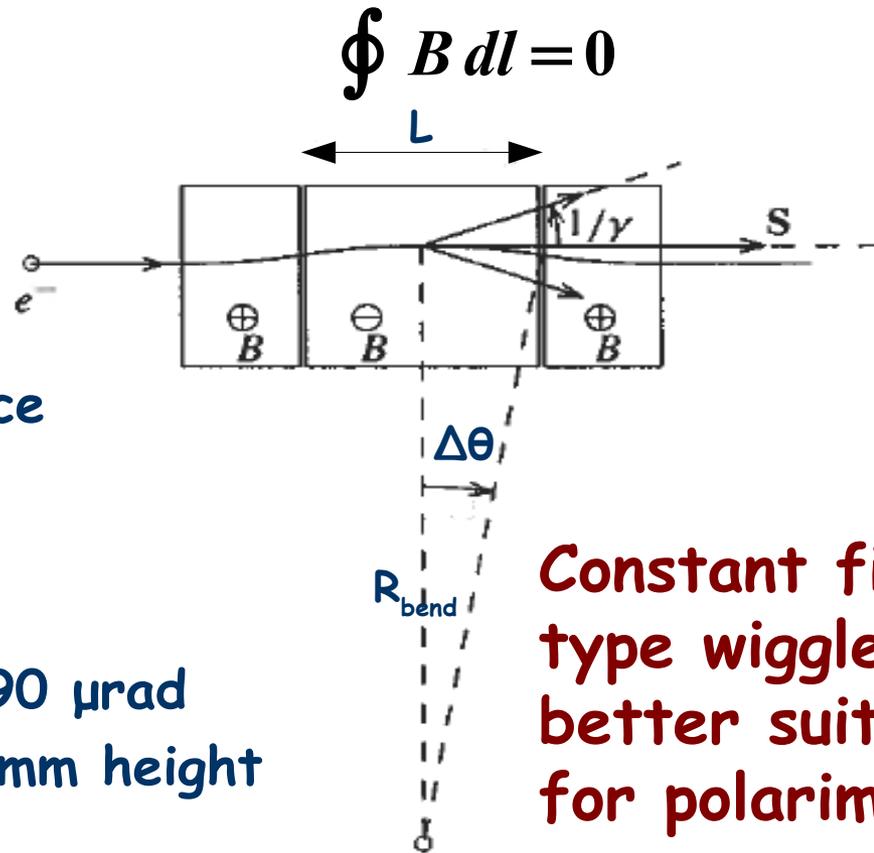
A Source of Spin Light: a 3 pole wiggler

$$R_{bend} = \frac{\gamma m_e c}{e B}$$

$$L = R_{bend} \Delta \theta$$

Horizontal angular acceptance
 $\Delta \theta$ fixed to 10 mrad

For $E_e = 11 \text{ GeV}$, spot size = 90 μrad
 i.e. 10m from the source $\sim 1 \text{ mm}$ height



Constant field
 type wiggler
 better suited
 for polarimeter

Fluctuations in energy and depolarization due to wiggler is negligible

“Spin Light” Detector

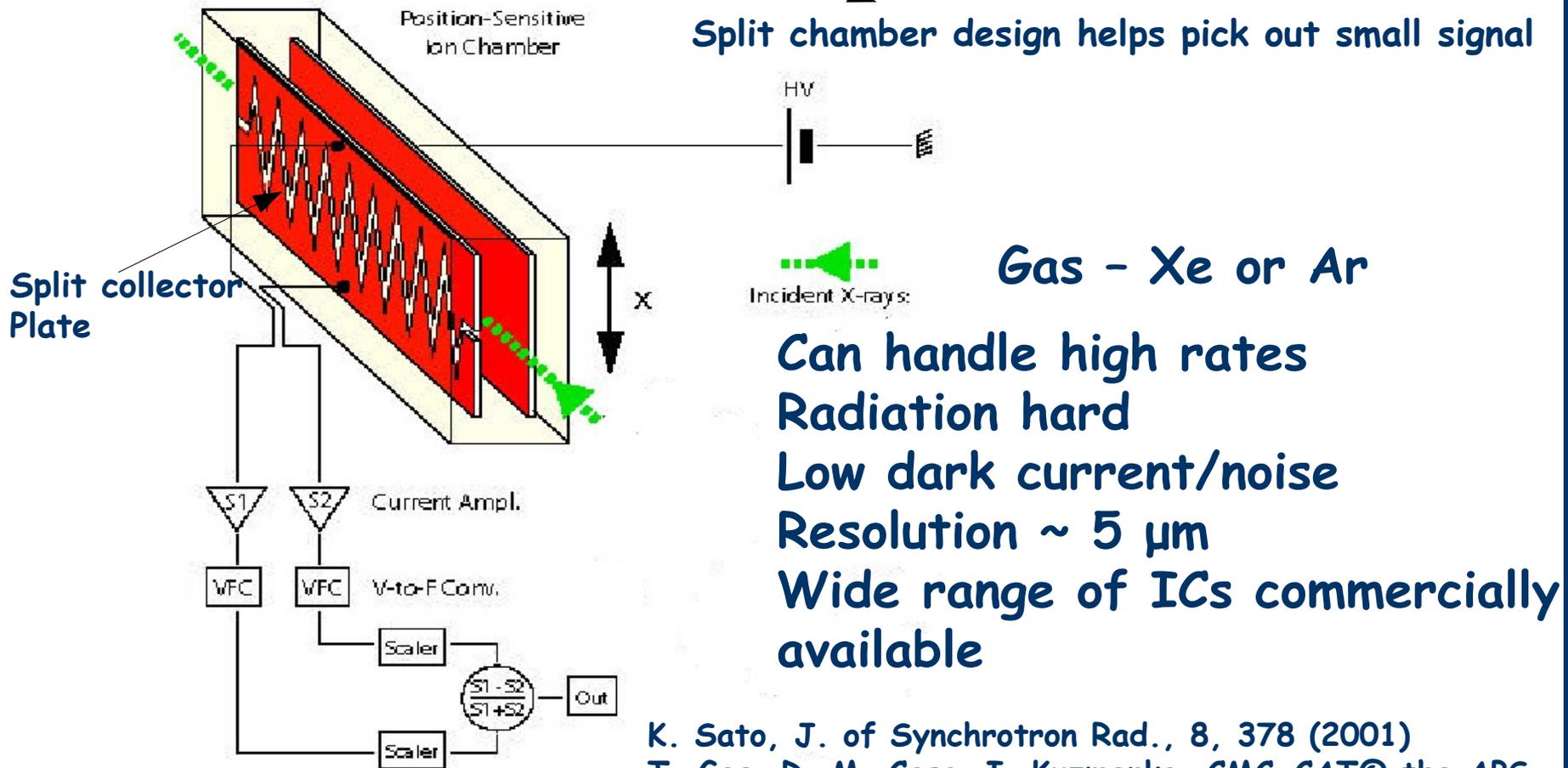
A Detector of Synchrotron + Spin light (X-rays)

A position sensitive differential ionization chamber

“Spin Light” Detector

A Detector of Synchrotron + Spin light (X-rays)

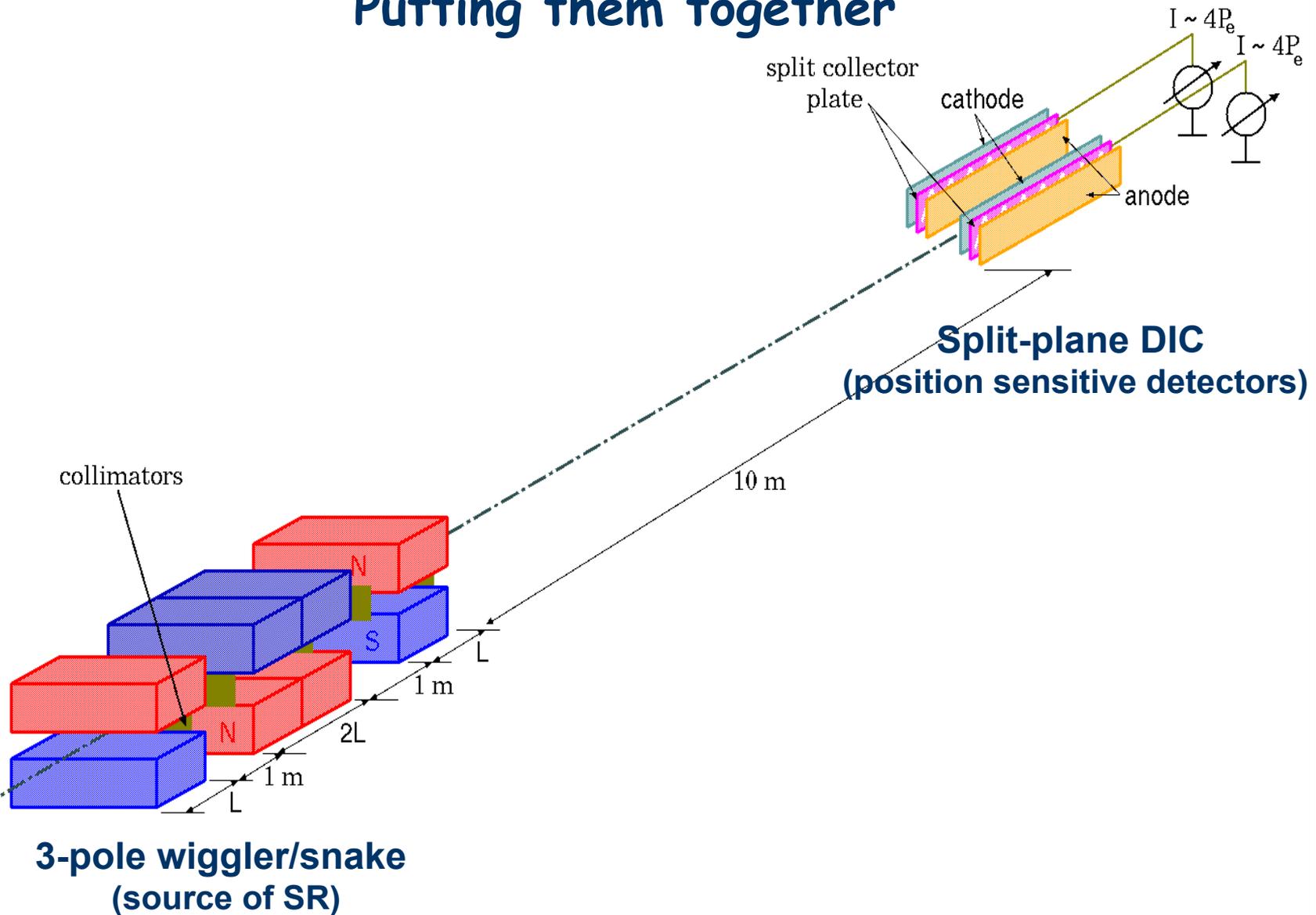
A position sensitive **differential** ionization chamber



K. Sato, J. of Synchrotron Rad., 8, 378 (2001)
T. Gog, D. M. Casa, I. Kuzmenko, CMC-CAT@ the APS

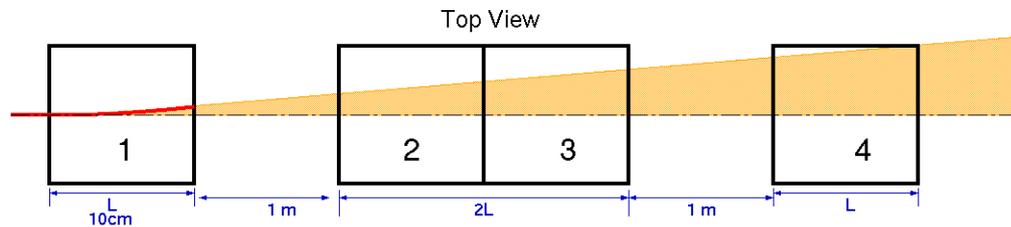
A “Spin Light” Polarimeter

Putting them together

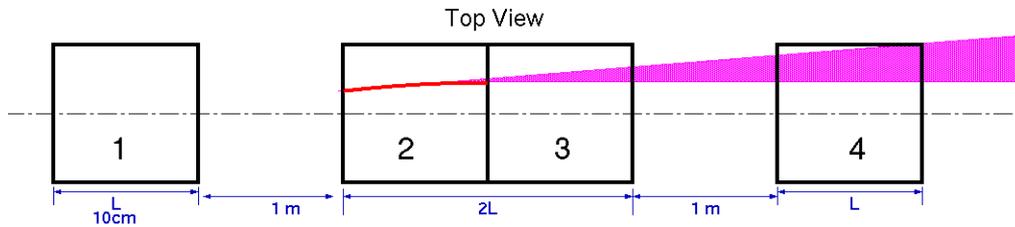


The SR from the Wiggler

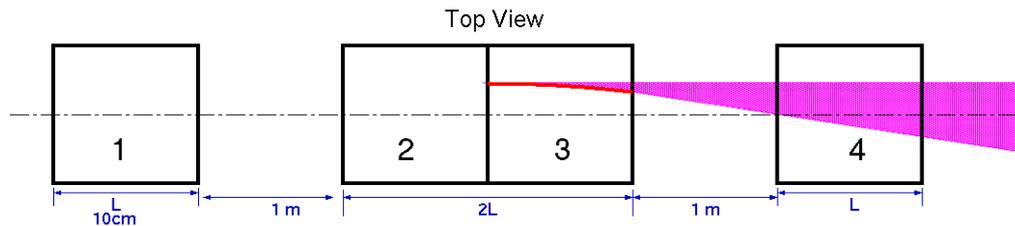
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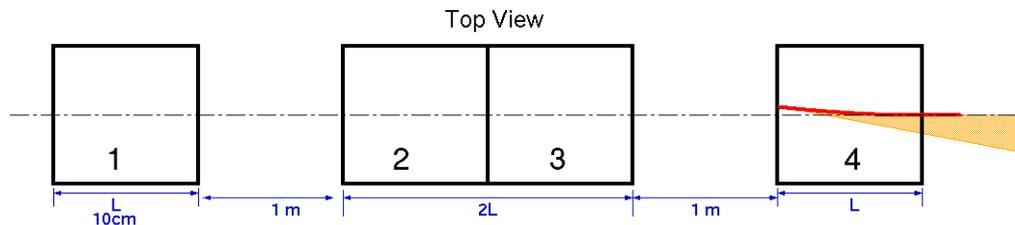
10 mrad Wiggler



10 mrad Wiggler



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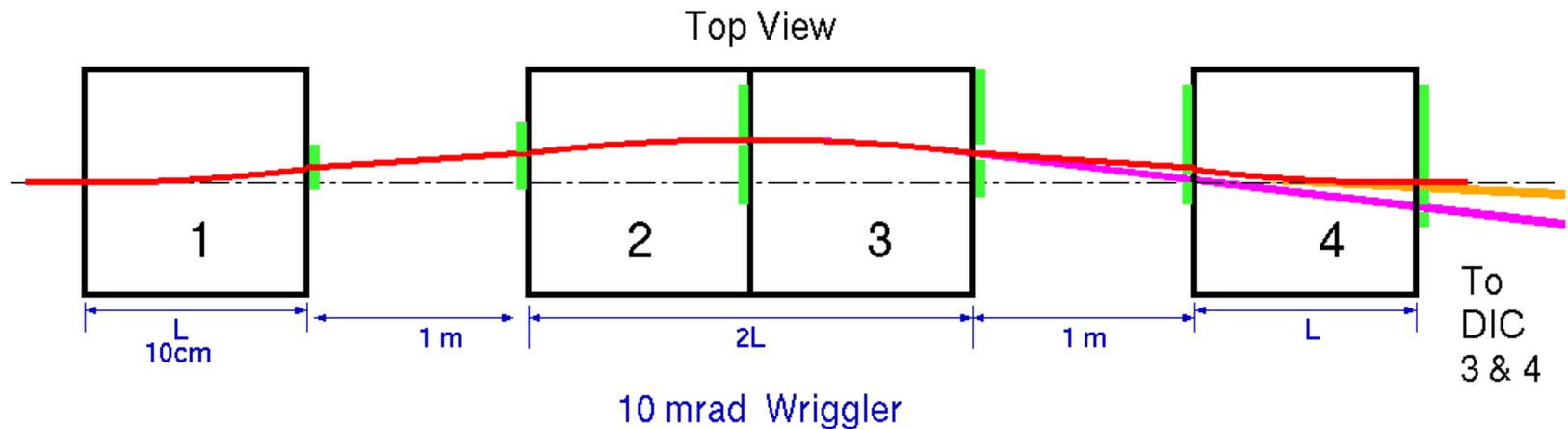
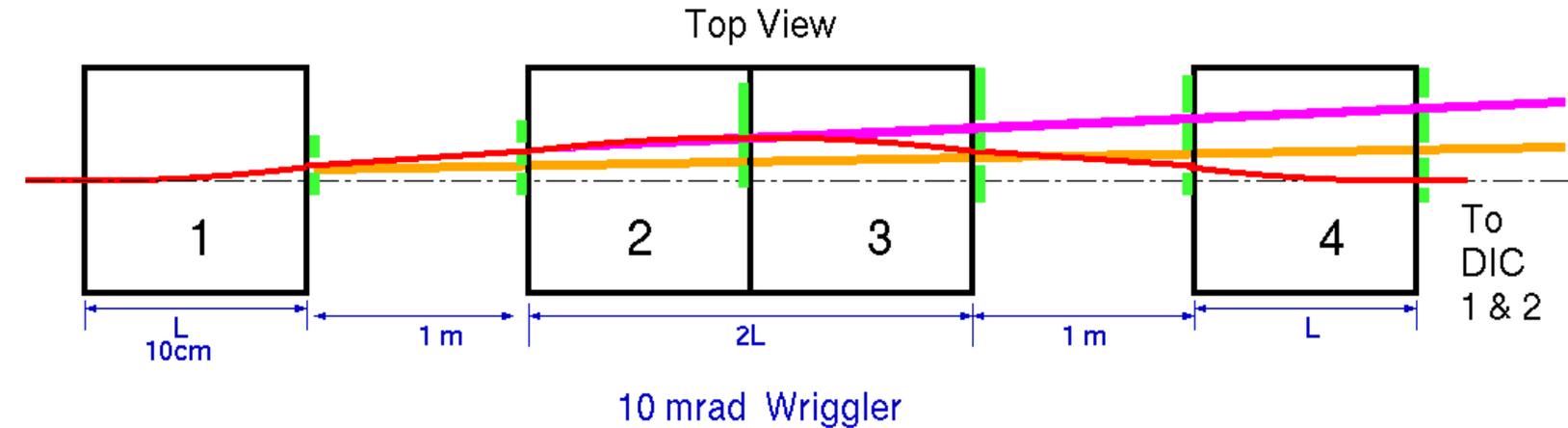


10 mrad Wiggler

**The SR fan
for each pole
of the wiggler**

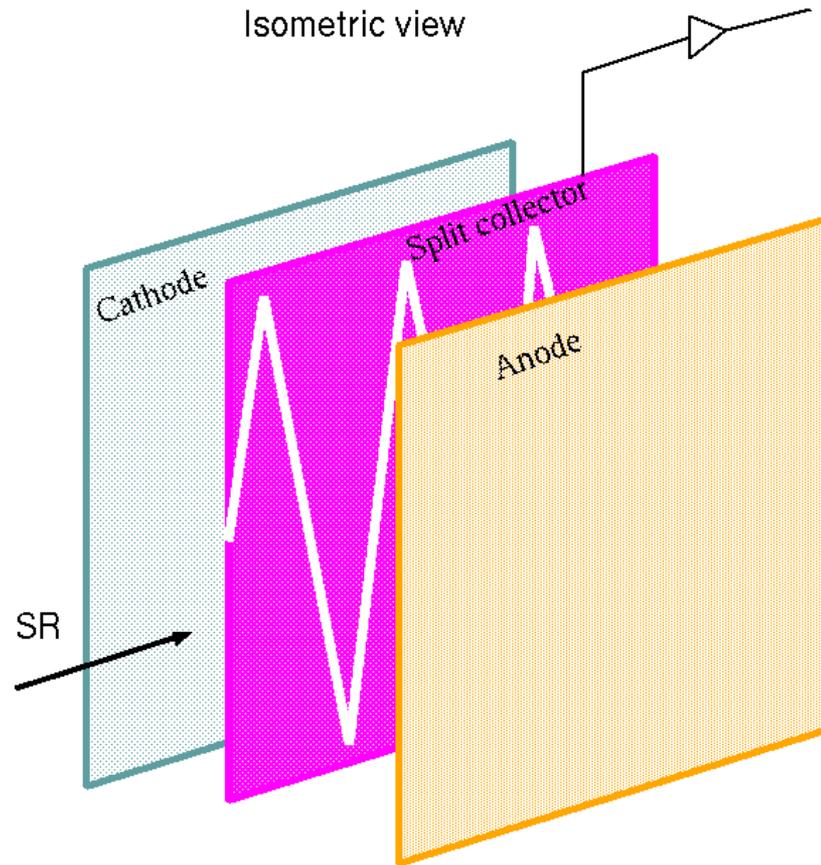
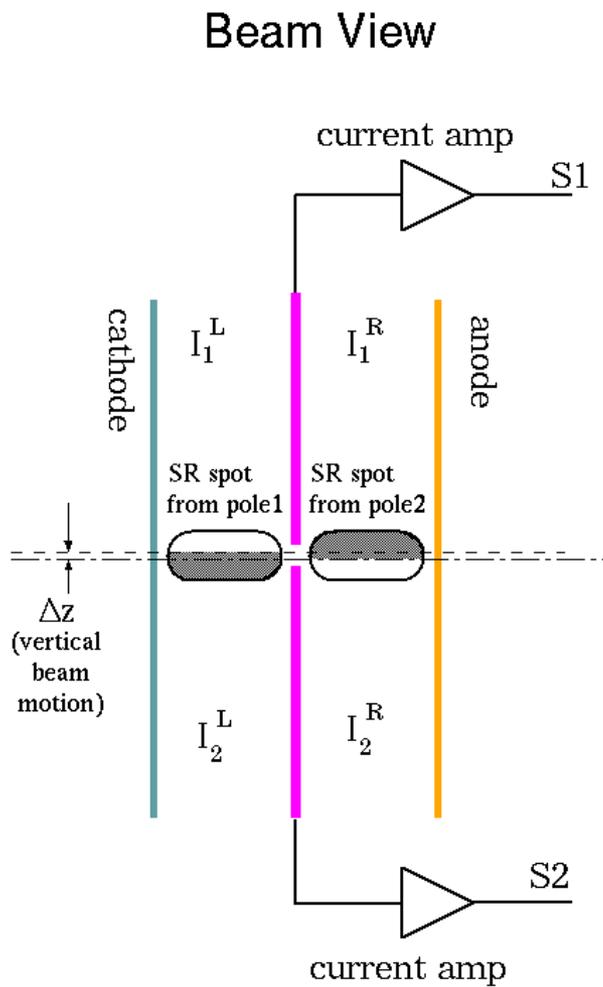
**The sign of the
asymmetry flips
for pole 2 and 3**

Collimating the SR



A set of slits select unique angular ranges for each pole

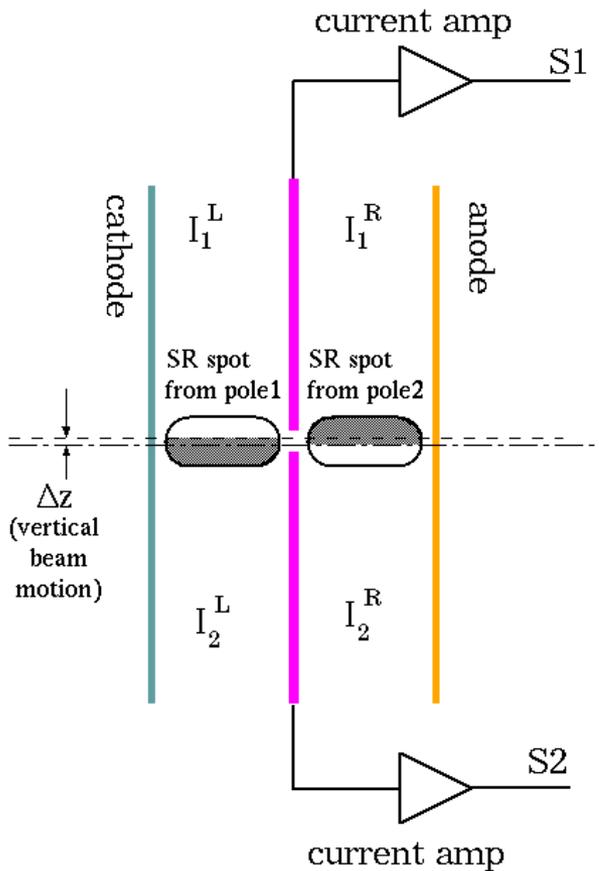
Detecting the Collimated SR



The Signal

DIC operated in current mode

Beam View



$$S1 = I_1^L + I_1^R$$

$$= (N_{SR}^L + \Delta N_{spin}^L + \Delta N_z^L) - (N_{SR}^R - \Delta N_{spin}^R + \Delta N_z^R)$$

Vertical beam motion cancels out

$$(S1 - S2) = 4\Delta N_{spin} \sim 4P_e$$

$$(S1 + S2) = 0$$

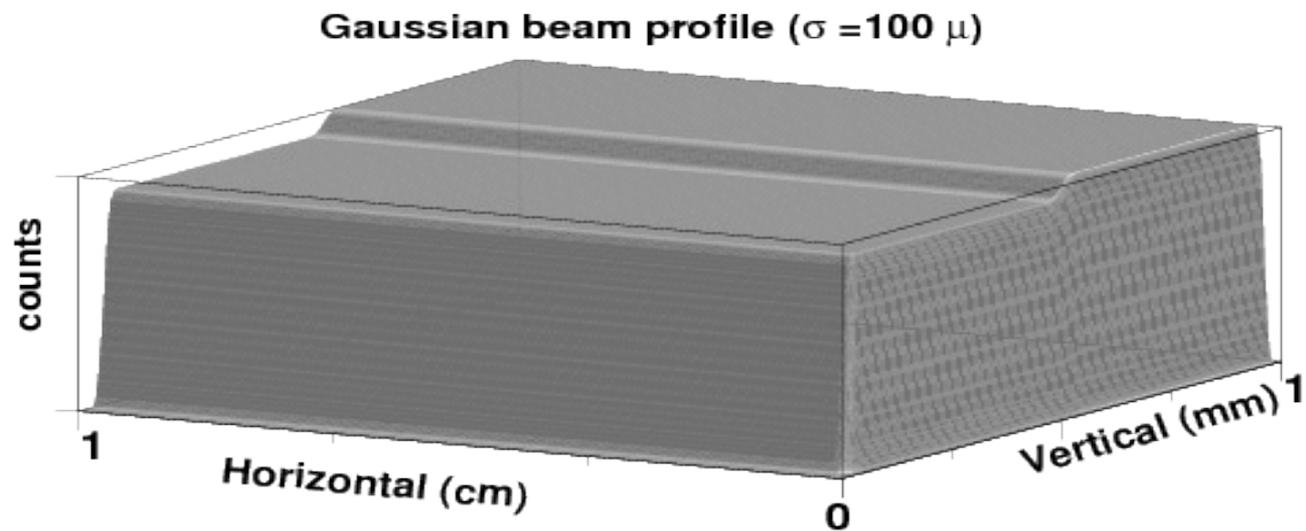
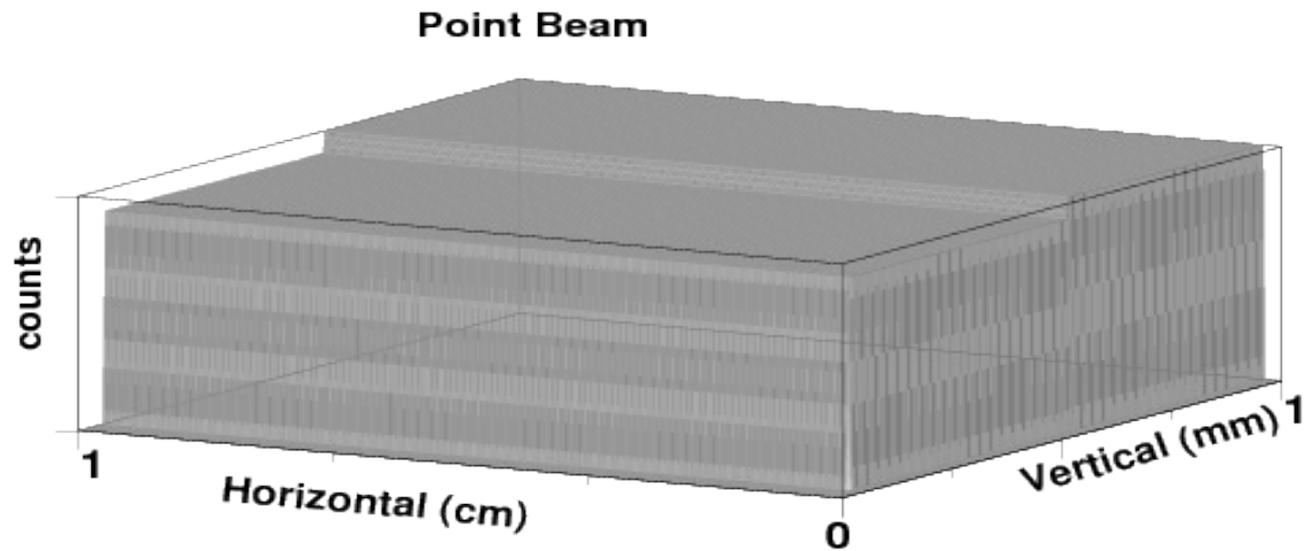
Vertical beam motion cancels out

$$S2 = I_2^L + I_2^R$$

$$= (N_{SR}^L - \Delta N_{spin}^L - \Delta N_z^L) - (N_{SR}^R + \Delta N_{spin}^R - \Delta N_z^R)$$

The sum S1+S2 can be used for systematic studies

Finite Beam Profile



Comparing Polarimetry Techniques

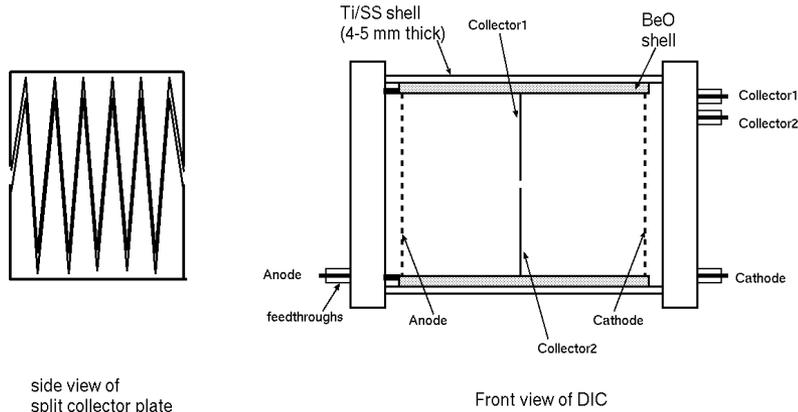
Sub-1% polarimetry requires multiple independent measurements of the beam polarization.

- **A Spin-light polarimeter is complimentary to the more popular Compton & Moller polarimeters.**
- **It will provide an independent measurement with completely different systematics**

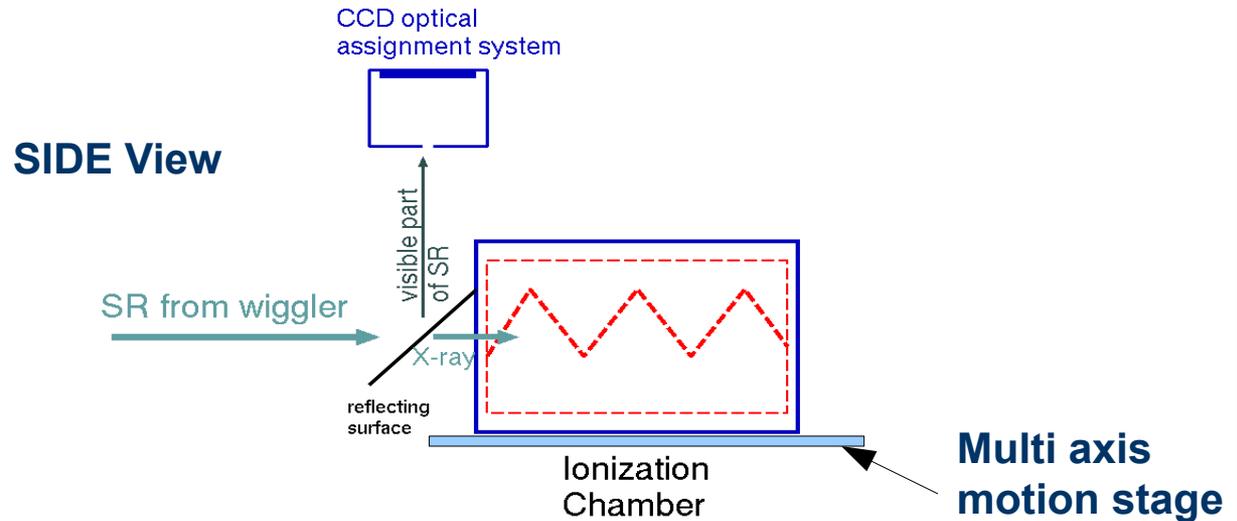
Compton	Spin-Light	Moller
Non-invasive/continuous	Non-invasive/continuous	invasive
Analyzing power is energy dependent	Analyzing power is energy dependent	Analyzing power is energy independent
Ideal for high currents	Ideal for high currents	Used at low currents only
Target is 100% polarized	No target needed	Target is <10% polarized
e & ν detection provide 2 independent polarimeters	2 sets of split plane DICs provide independent measurements	-

The Detector R&D Proposal

Stage1: Develop a split plane differential ionization chamber



Stage1: Develop a CCD based ionization chamber alignment system



The Detector R&D Proposal

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Stage 1: Test the DIC in the JLab Hall-A Compton chicane

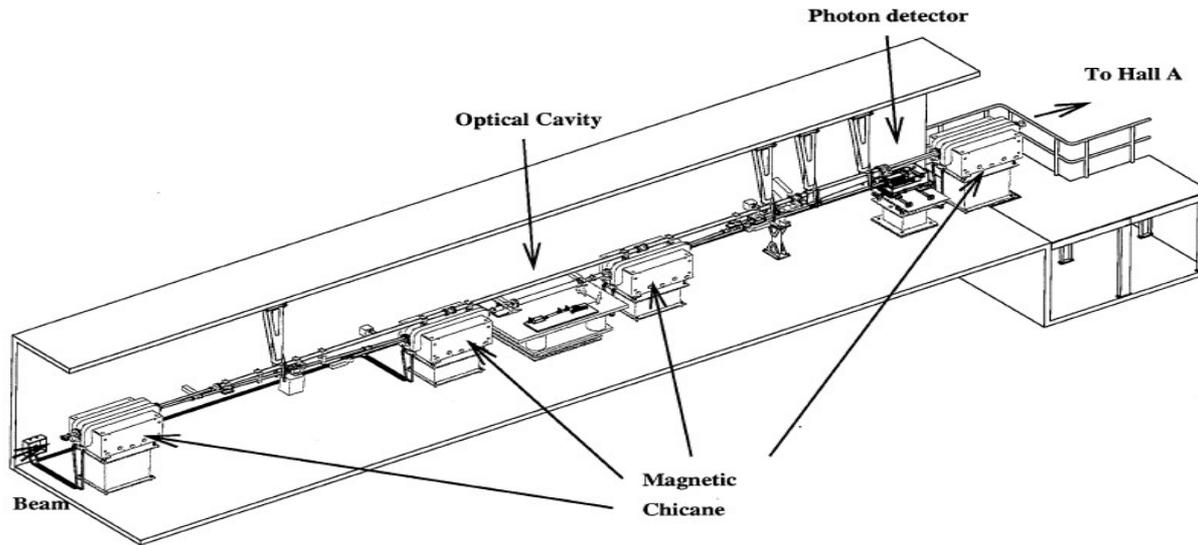


Fig. 14. The Compton Polarimeter Setup at TJNAF Hall A. Total length 15 m.

Stage 2: Develop a full prototype spinlight polarimeter (a set of dual ionization chambers and a suitable wiggler magnet.)

Students & Postdocs

The collaboration has extensive polarimetry and detector development experience at DESY, JLab, Mainz, and RHIC.

Grad. Students:

Edward Leggett (MSU) and **Valerie Gray** (W&M) and
MSI student(s) (Stony Brook U., during yrs. 2 and 3)

U. Grad: **Prajwal Mohanmurthy** (MSU, JSA research fellowship)

Post doc: **M. Shabestari** (MSU, 50% FTE only)

Funding Request

Item	Year 1	Year 2	Year 3	Total
0.5 Post-doc (MSU)	\$40k	\$40k	\$40k	\$120k
0.5 Grad student (W&M)	\$17k	\$17k	\$ 17k	\$51k
Equipment	\$46k	\$49k	\$48k	\$143k
Travel	\$10k	\$10k	\$10k	\$30k
Total	\$113k	\$116k	\$115k	\$344k

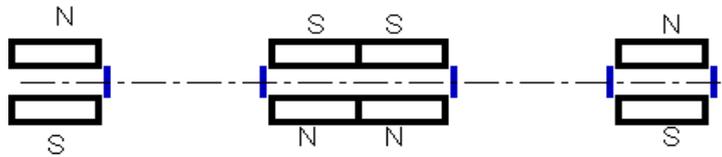
Summary

- Spin light based polarimeter is a viable option for precision non-invasive polarimetry
- It is based on a well demonstrated concept (for transversely polarized electrons), the necessary technology is readily available and widely used in light sources across the world.
- We propose to develop a split plane ionization chamber and demonstrate proof of principle for longitudinally polarized electrons using 12 GeV beam at JLab.
- Begin developing a full prototype spin light polarimeter

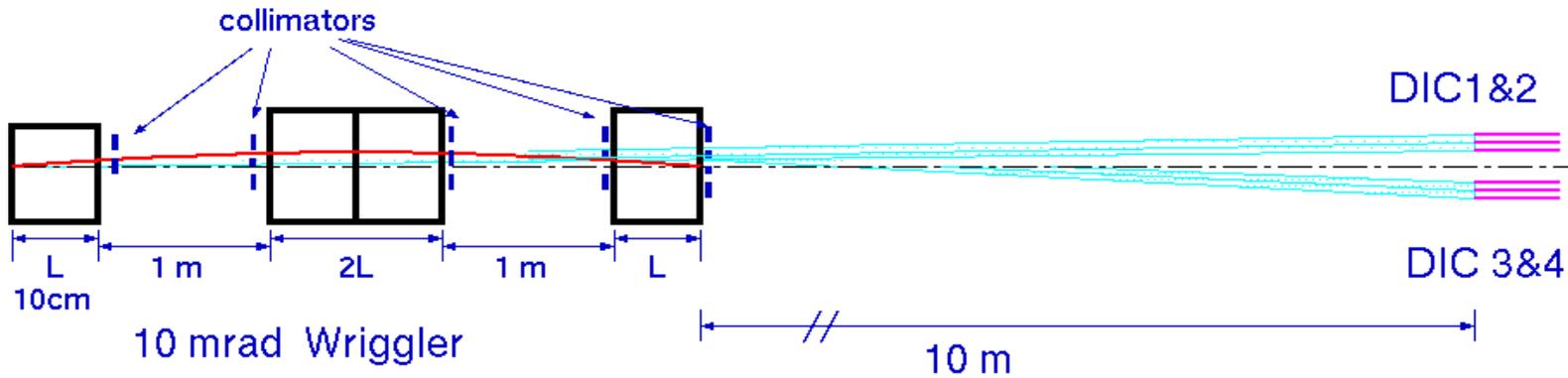
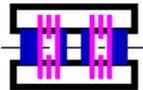
A "Spin Light" Polarimeter

A Recap

Front View



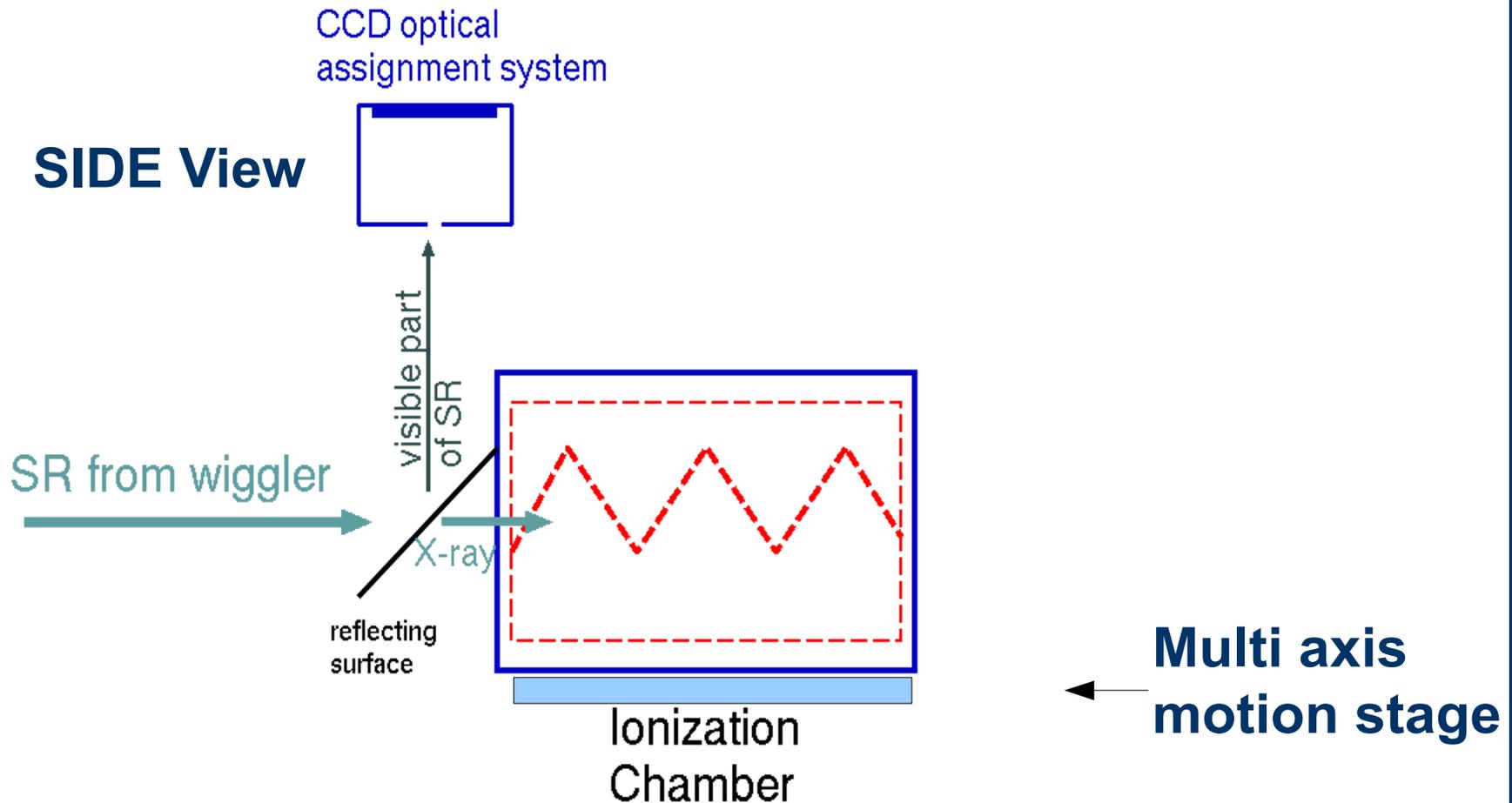
Side View



Top View

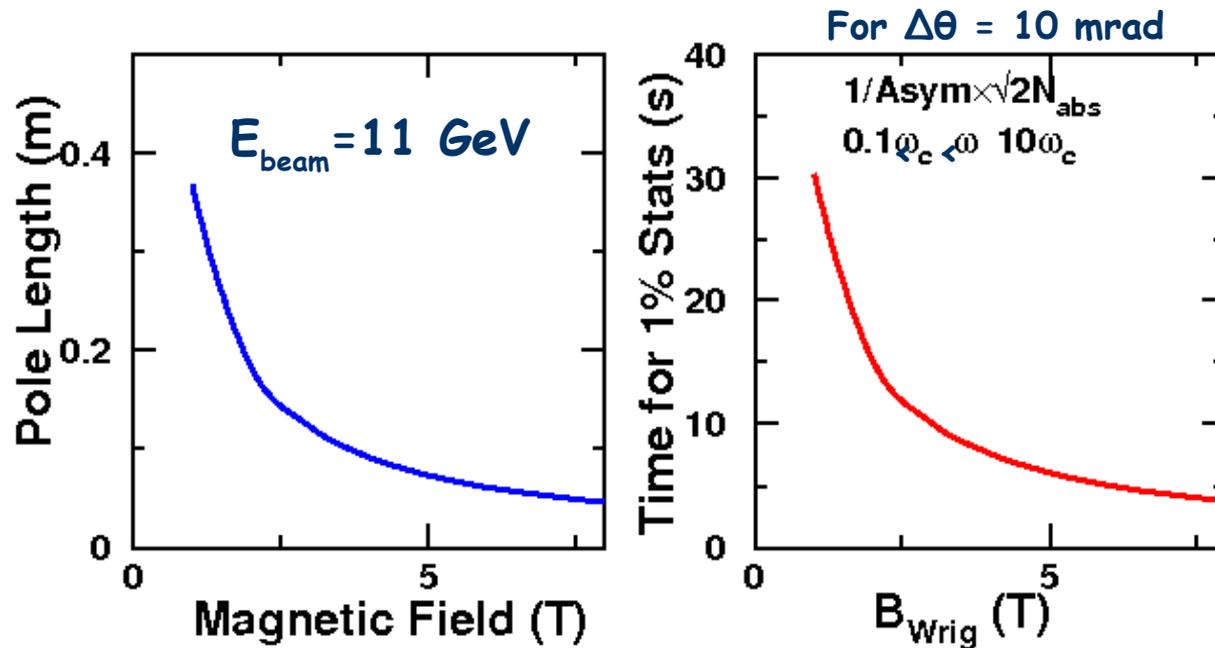
The Detector R&D Proposal

Stage 1: Develop a CCD based ionization chamber alignment system



Conceptual Design

Choosing the B_{wiggler}



Pole length and figure of merit have similar dependence on the B- field.

Choose $B = 4\text{T}$

The Proposal Timeline

Activity	Year 1	Year 2	Year 3
Design and build prototype DIC	✓	✓	
Test DIC in Hall A Compton beamline			✓
Design CCD based alignment system	✓	✓	
Design and build set of dual DIC			✓
Build CCD system			✓
Design wiggler magnet		✓	
Design slits and collimators		✓	
Identify suitable wiggler magnet at the APS			✓
Select suitable site to test prototype polarimeter			✓

The Detector R&D Proposal

Equipment	Total cost
prototype DIC	10000
Split plane electrodes	5000
Electronics for DIC(2 channels)	
current amps	8000
High voltage power supplies	10000
V-to-Fs and scalers	15000
VME crate	10000
Single board computer	7000
Gas Handling system	10000
The Dual DICs	
Custom dual DICs	12000
with split collector	
additional amps	8000
Custom beamline vacuum	10000
elements	
slits and collimators	8000
CCD alignment system	
motion stage, controller and driver (2)	16000
CCD imager and fast readout (2)	9000
light transport optics (2)	5000
Total Equipment Cost	143000

Table 1: Equipment cost breakup