

# The Quark-Parton Model and Low-Energy Factorization Studies in Semi-Inclusive Pion Production

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**Abstract.** A large set of  $\pi^\pm$  electroproduction cross sections from proton, deuterium and aluminum targets have been measured in Hall C. The data cover the range  $0.2 < x < 0.6$ ,  $2 < Q^2 < 4$  (GeV/c)<sup>2</sup>, and  $0.3 < z < 1$ , with transverse momenta  $P_t < 0.45$  GeV/c, and span the low energy residual-mass region. The cross section data have been used to construct a variety of ratios, in terms of favored to unfavored fragmentation functions, charged pion ratios and deuteron-hydrogen. The  $x$ ,  $z$  and  $P_t^2$  dependencies of the cross sections and their ratios (for  $W^2 > 4$  GeV<sup>2</sup> and  $z < 0.7$ ) show the features of factorization in a sequential electron-quark scattering and quark-pion fragmentation process. We find the azimuthal angular dependencies to be small. We find the intrinsic transverse momenta of the  $u$  quark to be slightly larger than for  $d$  quark, while the transverse momentum width of the favored and unfavored fragmentation functions is about the same, and are larger than the quark widths.

**Keywords:** Electroproduction, pion, quark, fragmentation, hadronization, duality, factorization

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## INTRODUCTION

In this report, we will concentrate on the low-energy domain of semi-inclusive electron scattering. Our focus will be on the process where a quark fragments into a pion, which carries away a large fraction of the exchanged virtual photon's energy.

In the  $eN \rightarrow e\pi^\pm X$  reaction, an electron with four-momentum  $(E, \vec{k})$  scatters from a nucleon with mass  $M$ , resulting in a scattered electron with four-momentum  $(E', \vec{k}')$ , exchanging a virtual photon with four-momentum  $q = (v, \vec{q})$  with a quark. A meson with four momentum  $(E_\pi, \vec{P}_\pi)$ , and transverse momentum  $P_t$  is produced. We define the four-momentum transfer squared as  $Q^2 = -q^2$  and Bjorken  $x$  as  $x = Q^2/2Mv$ . The fraction of the virtual photon energy taken away by the meson is  $z = E_\pi/v$ . If we neglect the pion mass, and if the meson is collinear with the  $\vec{q}$  and  $Q^2/v^2 \ll 1$ , we can present the square of mass of the undetected residual system as  $W'^2 = M^2 + Q^2(1-z)(\frac{1}{x} - 1)$ . Note, in the inclusive case, the square of the invariant mass is  $W^2 = M^2 + Q^2(\frac{1}{x} - 1)$ .

At high energies the cross section factorizes into the product of the virtual photon-quark interaction and the subsequent quark hadronization. A consequence of factorization is that the fragmentation function is independent of  $x$ , and the parton distribution function independent of  $z$ . At low energies, it is not obvious that the factorization holds.

The quark-hadron duality has been predicted [1], and verified [2] for high-energy meson electroproduction. While the phenomenon of duality in inclusive electron scattering is well-established, duality in the semi-inclusive meson electroproduction was not tested before this experiment. To investigate the existence of quark-hadron duality and its relation to low-energy factorization in semi-inclusive  $\pi^\pm$  electroproduction was one of the goals of the E00-108 experiment.

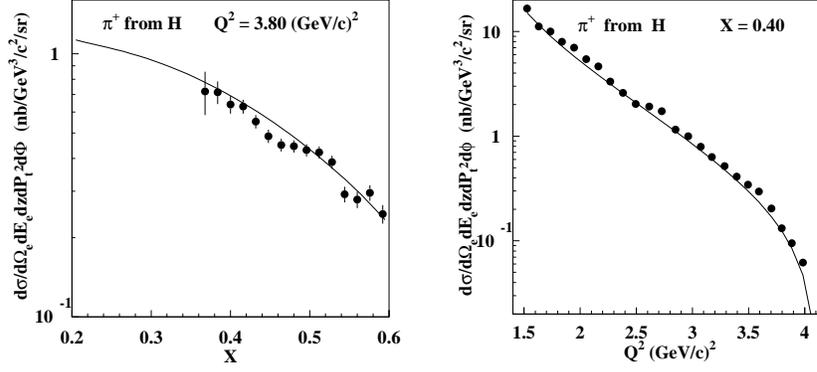
## EXPERIMENT

The experiment E00-108 [3] ran in 2003 in Hall C at JLab. Incident electrons, with energy of 5.479 GeV and currents 20 – 60  $\mu\text{A}$ , were scattered from 4-cm-long liquid hydrogen or deuterium targets and detected in the SOS spectrometer. The electroproduced pions were detected in the HMS spectrometer. The experiment consisted of three parts: i) at a fixed electron kinematics of  $(x, Q^2) = (0.32, 2.30 \text{ (GeV}/c)^2)$ ,  $z$  was varied from 0.3 to 1 by changing the HMS momentum from 1.3 to 4.1 GeV/ $c$ , with nearly uniform coverage in the pion azimuthal angle,  $\phi$ , around the  $\vec{q}$  direction, but at a  $\langle P_t \rangle \approx 0.05 \text{ GeV}/c$  ( $z$ -scan); ii) for  $z = 0.55$ ,  $x$  was varied from 0.2 to 0.6, with a corresponding variation in  $Q^2$  from 1.5 to 4.6  $(\text{GeV}/c)^2$ , by changing the SOS angle, keeping the pion centered on the  $\vec{q}$  direction ( $x$ -scan); iii) for  $(x, Q^2) = (0.32, 2.30 \text{ (GeV}/c)^2)$ ,  $z \approx 0.55$ ,  $P_t$  was scanned from 0 to 0.4 GeV/ $c$  by increasing the HMS angle (with  $\langle \phi \rangle \approx 180^\circ$ ) ( $P_t$ -scan).

## EXPERIMENTAL RESULTS

Many of the results are described in detail in [2, 4, 5]. We observed for the first time the quark-hadron duality phenomenon and the onset of low-energy factorization in semi-inclusive pion electroproduction. We compared the measured  $^{1,2}\text{H}(e, e'\pi^\pm)\text{X}$  cross sections as a function of  $z$  (at  $x = 0.32$ ) with the parton model calculation assuming CTEQ5M parton distribution functions [6] and the parametrized fragmentation functions of Binnewies, Kniehl and Kramer [7]. We found good agreement between data and model for  $z < 0.65$ . We constructed several ratios of cross sections off proton and deuteron targets, and found the ratio of fragmentation functions  $D^-/D^+$  to closely resemble that of high-energy reactions. We studied the cross sections as a function of the  $P_t^2$  in the context of a simple model, allowing separate widths for up ( $\mu_u$ ) and down ( $\mu_d$ ) quarks, and for favored ( $\mu_+$ ) and unfavored ( $\mu_-$ ) fragmentation functions, and assuming Gaussian distributions. We fit the  $P_t$ -dependence of the  $\pi^\pm$  cross sections for hydrogen and deuterium for the four widths, and the  $D^-/D^+$  and  $d/u$  ratios. We find the ratio  $d/u = 0.39 \pm 0.03$ , and  $D^-/D^+ = 0.43 \pm 0.01$ , in good agreement with the high energy data, and the width squared for  $u$  quarks  $\mu_u^2 = 0.07 \pm 0.03 \text{ (GeV}/c)^2$ . But for the  $d$ -quark width squared the fit gives value consistent with zero ( $\mu_d^2 = -0.01 \pm 0.05 \text{ (GeV}/c)^2$ ), and nearly similar values for the fragmentation widths ( $\mu_+^2 = 0.18 \pm 0.02 \text{ (GeV}/c)^2$  and  $\mu_-^2 = 0.14 \pm 0.02 \text{ (GeV}/c)^2$ ).

At  $z = 0.55$ , we have studied the  $x$ - and  $Q^2$ - dependencies of the  $^{1,2}\text{H}(e, e'\pi^\pm)\text{X}$  cross sections. We found good agreement between the data and model, as shown in Fig. 1 (left panel) for the  $x$ -dependence of the  $\pi^+$  cross sections at  $Q_{set}^2 = 3.8 \text{ (GeV}/c)^2$ . To study the



**FIGURE 1.** The  ${}^1\text{H}(e,e'\pi^+)X$  cross section. Left: As a function of  $x$  at  $z = 0.55$ ,  $Q_{\text{set}}^2 = 3.80$   $(\text{GeV}/c)^2$ . Right: As a function of  $Q^2$  at  $x = 0.40$ ,  $z = 0.55$ . The curves are the quark-parton model calculations.

$Q^2$ -dependence of the cross sections, we bin centered in  $x$  to a common  $x = 0.40$ . The  ${}^1\text{H}(e,e'\pi^+)X$  cross section versus  $Q^2$  is shown in the right panel of Fig. 1. The parton model calculations describe our data remarkably well.

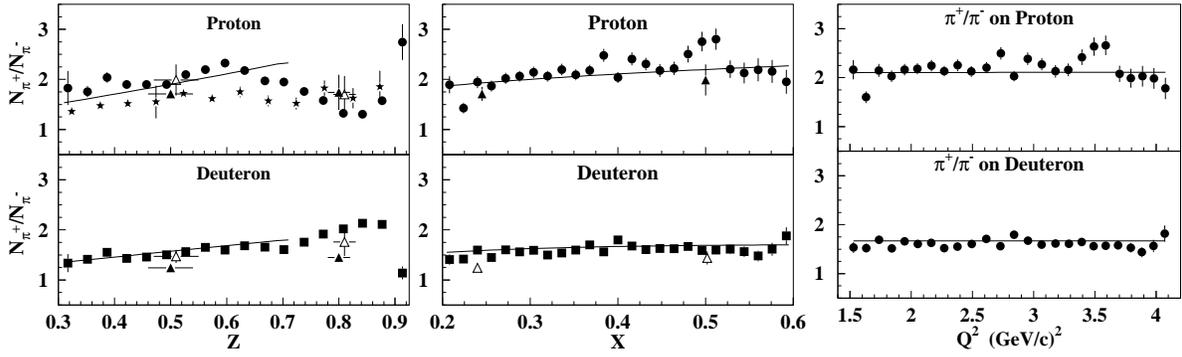
In Fig. 2 the  $\pi^+/\pi^-$  ratios are shown as functions of  $z$  (at  $x = 0.32$ ),  $x$  and  $Q^2$  (at  $z = 0.55$ ). The solid and open triangles are Cornell data [8] at  $(x, Q^2) = (0.24, 2.0$   $(\text{GeV}/c)^2)$  and  $(0.50, 4.0$   $(\text{GeV}/c)^2)$ , respectively. Stars represent HERMES data [9] at average values of  $\langle Q^2 \rangle = 2.5$   $(\text{GeV}/c)^2$ ,  $\langle W^2 \rangle = 28.6$   $\text{GeV}^2$ ,  $\langle \nu \rangle = 16.1$   $\text{GeV}$  and  $\langle x \rangle = 0.082$ . The solid line is the quark-parton model calculation. The  $\pi^+/\pi^-$  ratio from the proton is larger than those reported by HERMES, but agrees well with the Cornell data, and is consistent to the rise in  $z$  as expected from the quark-parton model calculation up to  $z \approx 0.6$ . For  $0.65 < z < 0.85$ , the ratio decreases because the  $\pi^- \Delta^{++}$  cross section is larger than the  $\pi^+ \Delta^0$  one. The sharp rise of the ratio at  $z > 0.85$  is due to exclusive  $\pi^+$  production. Similarly the deuteron also reproduces the expected rise from the quark-parton model calculation. At  $z > 0.7$  we see again effects rising from the  $N - \Delta$  transition.

In the central panel of Fig. 2 we show the  $\pi^+/\pi^-$  ratio versus  $x$  for proton (top) and deuterium (bottom) targets. Solid and open triangles represent data from Cornell [8] at  $(x, Q^2) = (0.24, 2.0$   $(\text{GeV}/c)^2)$ , and  $(0.50, 4.0$   $(\text{GeV}/c)^2)$ . Our  $\pi^+/\pi^-$  ratios is in good agreement with the Cornell data and with the quark-parton model prediction.

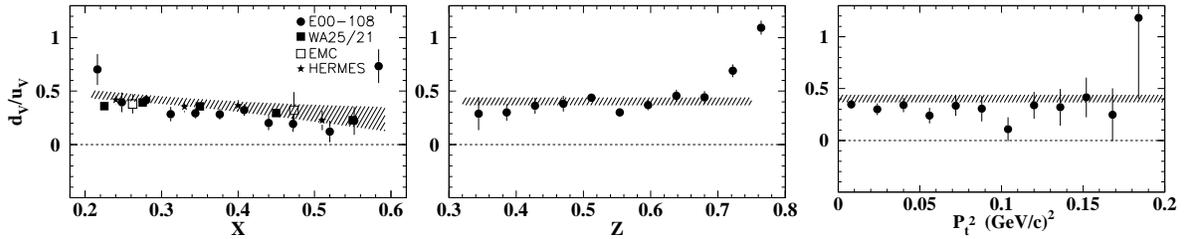
The  $\pi^+/\pi^-$  ratio versus  $Q^2$  (at  $z = 0.55$ ) shown in right panel of Fig. 2, agrees well with the quark-parton model expectations.

If factorization, isospin symmetry and charge conjugation holds, the  $\pi^\pm$  cross sections on the proton and deuteron can be used to extract the  $d_v/u_v$  ratio of valence quarks ( $u_v = u - \bar{u}$ , and  $d_v = d - \bar{d}$ ). This ratio is shown in Fig. 3, as a function of  $x$  (at  $z=0.55$ ),  $z$  (at  $x = 0.32$ ) and  $P_t^2$  (at  $x = 0.32$  and  $z = 0.55$ ). Our data are in good agreement with WA21/25 [10] and EMC [11] results, but below the HERMES data [12]. The ratio  $d_v/u_v$  may contain  $z$ -dependent factors, if the symmetry breaks down. One can witness in Fig. 3 (central panel) a sharp increase of the  $d_v/u_v$  ratio at  $z > 0.7$  where the  $\Delta$  transition comes into play. There is no apparent  $P_t$ -dependence of the ratios as can be seen in the right panel, although future higher-precision data are required to rule out any dependence.

We believe our work will provide a fruitful basis for future studies of the quark-parton model and more sophisticated model calculations at relatively low energies.



**FIGURE 2.** The ratio  $\pi^+/\pi^-$  for proton (top) and deuteron (bottom) targets. Left:  $\pi^+/\pi^-$  as a function of  $z$ , at  $x = 0.32$ . Solid and open triangles are Cornell data [8], and stars are HERMES data [9]. Center: Ratio  $\pi^+/\pi^-$  as a function of  $x$  at  $z = 0.55$ . Solid and open triangles are Cornell data [8]. Right: The ratio  $\pi^+/\pi^-$  as a function of  $Q^2$  for  $x = 0.4$  and  $z = 0.55$ . The lines are the quark-parton model expectations.



**FIGURE 3.** Left: The ratio of valence quarks  $d_v/u_v$  as a function of  $x$  at  $z=0.55$ . Solid and open squares represent data from WA-21/25 [10] and EMC [11]. Solid triangle symbols are HERMES data [12]. Center: The  $d_v/u_v$  as a function of  $z$  at  $x=0.32$ . Right: The ratio  $d_v/u_v$  as a function of  $P_t^2$  at  $x=0.32$  and  $z=0.55$ . The band is a quark-parton model expectation using CTEQ parton distribution function parameterizations [6].

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